

# min-xor

Consider two integers a and b. Their bitwise xor (exclusive or) is computed as it follows:

- Write each of them in binary:  $a = \overline{a_{k-1}a_{k-2}...a_0}$  and  $b = \overline{b_{k-1}b_{k-2}...b_0}$ ;
- Their bitwise xor, denoted by  $a \wedge b$ , has a bit equals to 1 in the position p if and only if exactly one of  $a_p$  and  $b_p$  has a value of 1.

For example,  $9 ^ 3 = 10$  because  $9 = 1001_{(2)}$ ,  $3 = 0011_{(2)}$  and  $10 = 1010_{(2)}$ .

### Task

You are given a sequence of N operations on a set of integers. The set is initially empty. Each operation can be one of the following:

- 1. insert(x): append integer x to the set;
- 2. delete(x): remove integer x from the set;
- 3. *min-xor()*: print the smallest bitwise xor between any two integers currently in the set.

You must print the output from every *min-xor()* operation.

## Input data

The first line of the input file minxor.in contains the number of operations N. Each of the following lines describes an operation using the following syntax:

1 x for insert(x)
2 x for delete(x)
3 for min-xor()

#### **Output data**

The output file minxor.out must contain a number of lines equals to the number of *min-xor()* operations. Each line must contain a single number, the answer to the corresponding *min-xor()* operation.

#### **Limits and constraints**

- $1 \le N \le 100,000$ ;
- $1 \le x \le 1,000,000,000$  for all *insert(x)* and *delete(x)* operations;
- For any insert(x) operation it is guaranteed that x does not exist in the set;
- For any *delete(x)* operation it is guaranteed that *x* exists in the set;
- For any *min-xor()* operation it is guaranteed that the set has at least 2 elements;
- Time limit: 0.4 second
- Memory limit: 8 MB



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# Example

minxor.in	minxor.out	Explanations
10	9	For the first <i>min-xor()</i> , the set is {24, 17}. The minimum bitwise
1 24	6	$xor is 24 ^ 17 = 9.$
1 17	6	
3	15	For the second $min$ - $xor()$ , the set is $\{24, 17, 23, 30\}$ . The
1 23		minimum bitwise xor is $24 ^30 = 6$ (also $17 ^23 = 6$ ).
1 30		For the third <i>min-xor()</i> , the set is {24, 23, 30}. The minimum
3		
2 17		bitwise xor is $24 \wedge 30 = 6$ .
3		
2 30		For the last $min$ - $xor()$ , the set is $\{24, 23\}$ . The minimum bitwise
3		$xor is 24 ^ 23 = 15.$